

# THEORY OF COMPUTATION AND COMPILERS

## Unit - III

### SEMANTIC ANALYSIS, INTERMEDIATE CODE GENERATOR & SYMBOL TABLE

#### SEMANTIC ANALYSIS



- Attributed Grammars
- Syntax Directed Translation

#### INTERMEDIATE CODE GENERATOR

- Intermediate Forms of Source Programs - Abstract Syntax Tree, Polish Notation and Three Address Codes
- Intermediate Code Forms
- Type Checker

#### SYMBOL TABLE

- Symbol Table Format
- Organization for Block Structures Languages
- Hashing

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# SEMANTIC ANALYSIS

## Syntax-Directed Translation (SDT)

3.1.1. Syntax-Directed Definitions (SDD)

3.1.2. Evaluation Orders for SDD's

3.1.3. Applications of Syntax-Directed Translation

3.1.4. Syntax-Directed Translation Schemes

# Syntax Analysis

## Syntax-Directed Translation (SDT)

### Syntax-Directed Definitions (SDD)

- Inherited and Synthesized Attributes
- Evaluating an SDD at the Nodes of a Parse Tree

# Semantic Analysis

- Let us concentrate on the third phase of the **compiler** called **semantic analysis**.
- The main goal of the **semantic analysis** is to **check the correctness of program** and **enable proper execution**.
- We know that the job of the **parser** is only to **verify that the input program** consists of **tokens** arranged on **syntactically valid** combination.
- In **semantic analysis** we check whether they form a **sensible set of instructions** in the **programming language**.

# Semantic Analysis

## Definition:

- **Semantic analysis** is the **third phase** of the **compiler** which acts as an **interface between syntax analysis phase** and **code generation phase**.
- It accepts the **parse tree** from the **syntax analysis** phase and adds the **semantic information** to the **parse tree** and performs certain **checks** based on this information.
- It also helps constructing the **symbol table** with appropriate information.

# Semantic Analysis

Some of the actions performed semantic analysis phase are:

- **Type checking** i.e., number and type of arguments in function call and in function header of function definition must be same. Otherwise, it results in semantic error.
- **Object binding** i.e., associating variables with respective function definitions.
- **Automatic type conversion** of integers in mixed mode of operations.
- Helps in **intermediate code generation**.
- Display appropriate **error messages**.

# Semantic Analysis

The **semantics of a language** can be described very easily using two notations namely:

- **Syntax Directed Definition (SDD)**
- **Syntax Directed Translation (SDT)**

**Note:** Consider the production  $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{T}$ . To distinguish  $\mathbf{E}$  on **LHS** of the production and  $\mathbf{E}$  on **RHS** of the production, we use  $\mathbf{E}_1$  on **RHS** of the production as shown below:

$$\mathbf{E} \rightarrow \mathbf{E}_1 + \mathbf{T}$$

# Semantic Analysis

Let us consider the **production**, its **derivation** and corresponding **parse tree** as shown below:

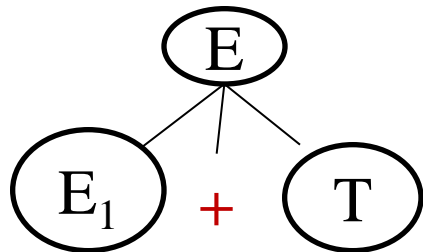
**Production:**

$$E \rightarrow E_1 + T$$

**Derivation:**

$$E \Rightarrow E_1 + T$$

**Parse Tree:**





# Semantic Analysis

- The non-terminal **E** on **LHS** of the production is called “**head of the production**”.
- The string of grammar symbols “**E<sub>1</sub> + T**” on **RHS** of the production is called “**body of the production**”.
- So, in the **derivation**, **head of the production** will be the **parent node** and the symbols that represent **body of the production** will be the **children nodes**.

# Syntax Directed Definition (SDD)

## Definition:

A **Syntax Directed Definition (SDD)** is a **context free grammar** with **attributes** and **semantic rules**. The **attributes** are associated with **grammar symbols** whereas the **semantic rules** are associated with **productions**. The **semantic rules** are used to **compute the attribute values**.

# Syntax Directed Definition (SDD)

## Example:

A simple **Syntax Directed Definition (SDD)** for the production  $E \rightarrow E_1 + T$  can be written as shown below:

Production	Semantic Rule
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$ Where <b>val</b> is <b>attribute</b>

Observe that a **semantic rule** is associated with **production** where the **attribute name val** is associated with each **non-terminal** used in the rule.

# Syntax Directed Definition (SDD)

## Attribute: Definition

An **attribute** is a property of a **programming language construct**. **Attributes** are always associated with **grammar symbols**. If **X** is a **grammar symbol** and '**a**' is the **attribute**, then **X.a** denote the **value of attribute 'a'** at a particular **node X** in the **parse tree**. If we implement the **nodes** of the **parse tree** by **records** or using **structures**, then the **attribute** of **X** can be implemented as a **field** in the **record** or a **structure**.

# Syntax Directed Definition (SDD)

## Attribute: Examples

- **Ex 1:** If *val* is the attribute associated with a non-terminal **E**, then **E.val** gives the value of attribute *val* at a node **E** in the parse tree.
- **Ex 2:** If *lexval* is the attribute associated with a terminal **digit**, then **digit.lexval** gives the value of attribute *lexval* at a node **digit** in the parse tree.
- **Ex 3:** If *syn* is the attribute associated with a non-terminal **F**, then **F.syn** gives the value of attribute *syn* at a node **F** in the parse tree.

# Syntax Directed Definition (SDD)

## Attribute:

### Typical examples of attributes are:

- The data types associated with variables such as **int**, **float**, **char** etc.
- The value of an **expression**
- The location of a **variable** in **memory**
- The **object code** of a **function** or **procedure**
- The number of **significant digits** in a **number** and so on.

# Syntax Directed Definition (SDD)

## Attributed Grammar: Definition

**Attribute grammar** is a special form of **context-free grammar** where some **additional information** (**attributes**) are appended to one or more of its **non-terminals** in order to provide **context-sensitive information**.

Each **attribute** has well-defined **domain of values**, such as **integer**, **float**, **character**, **string**, and **expressions**.

**Attribute grammar** is a **medium** to provide **semantics** to the **context-free grammar** and it can help specify the **syntax** and **semantics** of a **programming language**.

**Attribute grammar** (when viewed as a **parse-tree**) can pass **values** or **information** among the **nodes** of a tree. 15

# Syntax Directed Definition (SDD)

## Semantic rule: Definition

The **rule** that describe how to compute the **attribute values** of the **attributes** associated with a **grammar symbol** using **attribute values** of **other grammar symbols** is called **semantic rule**.

**For example**, consider the production  $E \rightarrow E_1 + T$ . The **attribute value** of **E** which is on **LHS** of the **production** denoted by **E.val** can be calculated by adding the **attribute values** of **variables E** and **T** which are on **RHS** of the **production** denoted by **E<sub>1</sub>.val** and **T.val** as shown below:

$$E.val = E_1.val + T.val \quad // \quad \text{Semantic rule}$$



# Inherited and Synthesized Attributes

The **attribute value** for a **node** in the **parse tree** may depend on information from its **children nodes** or its **sibling nodes** or **parent nodes**. Based on how the **attribute values** are obtained we can **classify the attributes**.

There are **two types of attributes** namely:

- **Synthesized attribute (S-attribute)**
- **Inherited attribute (I-attribute)**

# Inherited and Synthesized Attributes

## Synthesized Attribute (S-attribute) :

### *Definition :*

The **attribute value** for a **non-terminal A** derived from the **attribute values** of its **children** or itself is called **synthesized attribute**. Thus, the **attribute values** of **synthesized attributes** are passed up from **children** to the **parent node** in **bottom-up manner**.

# Inherited and Synthesized Attributes

## Synthesized Attribute (S-attribute):

### *Example:*

Consider the production:  $\mathbf{E} \rightarrow \mathbf{E}_1 + \mathbf{T}$ . Suppose, the attribute value `val` of  $\mathbf{E}$  on **LHS (head)** of the production is obtained by adding the attribute values  $\mathbf{E}_1.\mathbf{val}$  and  $\mathbf{T}.\mathbf{val}$  appearing on the **RHS (body)** of the production as shown below:

Production	Semantic Rule
$\mathbf{E} \rightarrow \mathbf{E}_1 + \mathbf{T}$	$\mathbf{E}.\mathbf{val} = \mathbf{E}_1.\mathbf{val} + \mathbf{T}.\mathbf{val}$

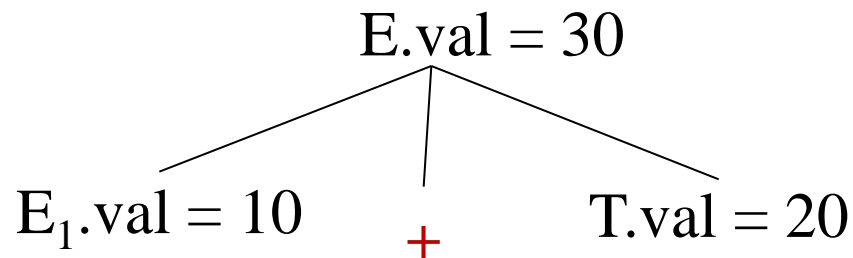
# Inherited and Synthesized Attributes

## Synthesized Attribute (S-attribute):

*Example:*

Production	Semantic Rule
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$

Parse tree with attribute values:

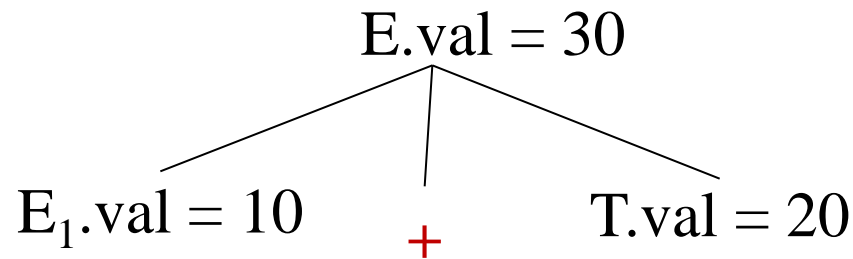


# Inherited and Synthesized Attributes

## Synthesized Attribute (S-attribute) :

*Example :*

**Parse tree with attribute values :**



Now, attribute **val** with respect to **E** appearing on **head of the production** is called **synthesized attribute**. This is because, the **value** of **E.val** which is **30**, is obtained from the **children** by **adding the attribute values 10 and 20** as shown in above **parse tree**.

# Inherited and Synthesized Attributes

## Inherited Attribute (I-attribute) :

### *Definition :*

The **attribute value** of a **non-terminal A** derived from the **attribute values** of its **siblings** or from its **parent** or **itself** is called **inherited attribute**. Thus, the **attribute values** of **inherited attributes** are passed from **siblings** or from **parent** to **children** in **top-down** manner.

# Inherited and Synthesized Attributes

## Inherited Attribute (I-attribute) :

### *Example :*

Consider the production:  $D \rightarrow T V$  which is used for a *single declaration* such as:

*int sum*

In the production,  $D$  stands for *declaration*,  $T$  stands for *type* such as *int* and  $V$  stands for the *variable* *sum* as in above declaration.

# Inherited and Synthesized Attributes

## Inherited Attribute (I-attribute):

### *Example:*

The production, semantic rule and parse tree along with attribute values are shown below:

Production	Semantic Rule
$D \rightarrow T V$	$V.inh = T.type$

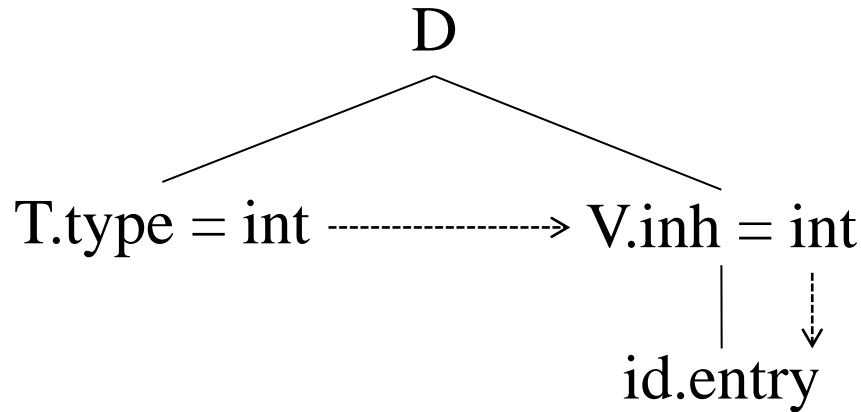


# Inherited and Synthesized Attributes

Inherited Attribute (I-attribute):

*Example:*

Parse tree with attribute values:



# Inherited and Synthesized Attributes

## Inherited Attribute (I-attribute) :

### *Example :*

Observe the following points from the above **parse tree**:

- The type **int** obtained from the **lexical analyzer** is already stored in **T.type** whose value is transferred to its **sibling V**. This can be done using:

$$\mathbf{V.inh = T.type}$$

Since attribute value for **V** is obtained from its **sibling**, it is **inherited attribute** and its **attribute** is denoted by **inh**.

# Inherited and Synthesized Attributes

## Inherited Attribute (I-attribute) :

### *Example :*

Observe the following points from the above **parse tree**:

- On similar line, the value **int** stored on **V.inh** is transferred to its **child id.entry** and hence **entry** is **inherited attribute** of **id** and attribute value is denoted by **id.entry**.

**Note :** With the help of the **annotated parse tree**, it is very easy for us to construct **SDD** for a given grammar.

# Inherited and Synthesized Attributes

## Annotated parse tree:

### *Definition:*

A parse tree showing the attribute values of each node is called *annotated parse tree*. The terminals in the *annotated parse tree* can have only synthesized attribute values and they are obtained directly from the lexical analyzer. So, there are no semantic rules in SDD (Syntax Directed Definition) to get the lexical values into terminals of the *annotated parse tree*. The other nodes in the *annotated parse tree* may be either synthesized or inherited attributes.

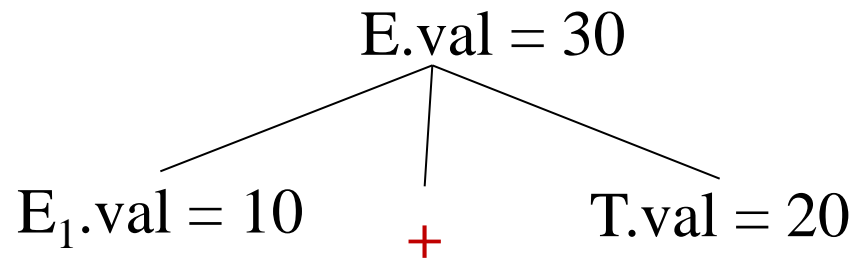
**Note:** Terminals can never have inherited attributes.

# Inherited and Synthesized Attributes

Annotated parse tree:

*Example:*

Consider the **partial annotated parse tree** shown below:



In the above **partial annotated parse tree**, the **attribute values 10, 20 and 30** are stored in  **$E_1.val$ ,  $T.val$  and  $E.val$**  respectively.

# Inherited and Synthesized Attributes

## Example-1:

Write the **SDD** for a simple desk calculator and show annotated parse tree for the expression  $(3+4)*(5+6)n$

**S** → **En**

**E** → **E + T | E - T | T**

**T** → **T \* F | T / F | F**

**F** → **( E ) | digit**

# Inherited and Synthesized Attributes

## Example: *Solution*

The given grammar is shown below:

$$S \rightarrow En$$
$$E \rightarrow E + T \mid E - T \mid T$$
$$T \rightarrow T * F \mid T / F \mid F$$
$$F \rightarrow ( E ) \mid \text{digit}$$

The above grammar generates an **arithmetic expression** consisting of **parenthesized** or **un-parenthesized expression** with operators **+** and **\***. For the sake of convenience, let us consider part of the grammar written as shown below:

# Inherited and Synthesized Attributes

**Example:** *Solution*

**S** → **T<sup>n</sup>**

**T** → **T \* F | T / F | F**

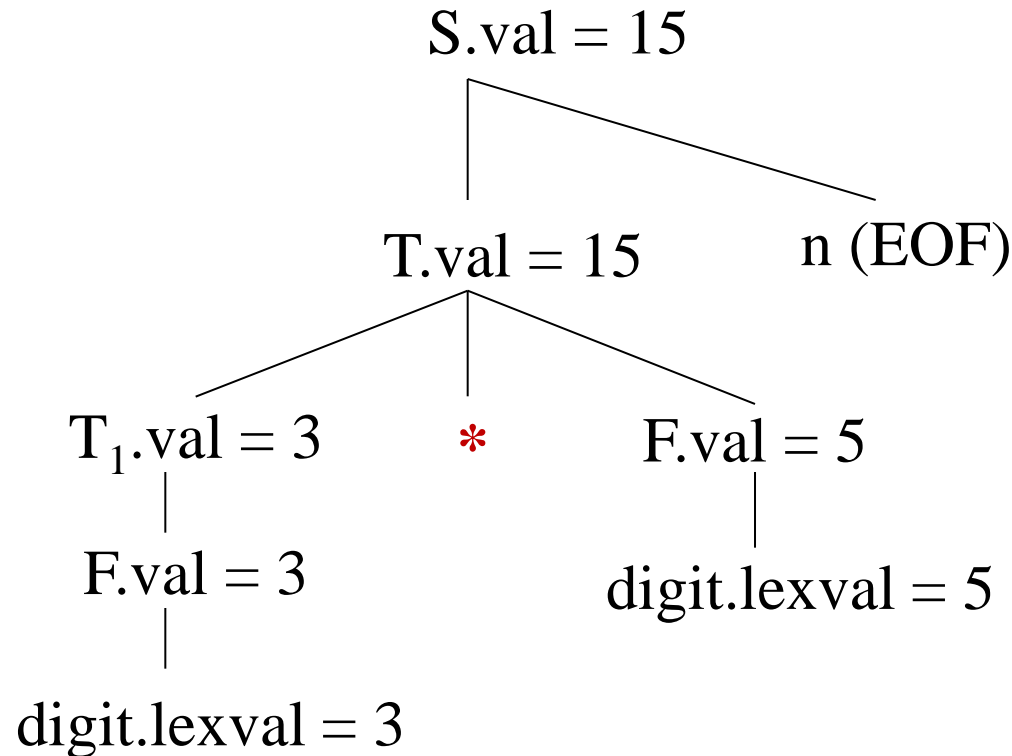
**F** → **digit**

Using the above productions we can generate an unparenthesized expression consisting of only **\*** operator such as: **3\*4** or **3\*4\*5** etc. The **annotated parse tree** for evaluating the expression **3\*5** is shown below:



# Inherited and Synthesized Attributes

**Example:** *Solution*



# Inherited and Synthesized Attributes

## Example: *Solution*

It is very easy to see how the values **3** and **5** are moved from bottom to top till we reach the root node to get the value **15**. The rules to get the value **15** from the productions used are shown below:

Productions	Semantic Rules
$F \rightarrow \text{digit}$	$F.val = \text{digit.lexval}$
$T \rightarrow F$	$T.val = F.val$
$T \rightarrow T_1 * F$	$T.val = T_1.val * F.val$
$S \rightarrow T_n$	$S.val = T.val$

# Inherited and Synthesized Attributes

## Example: *Solution*

On similar lines we can write the semantic rules for the following productions as shown below:

Productions	Semantic Rules
$S \rightarrow E_n$	$S.val = E.val$
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
$E \rightarrow T$	$E.val = T.val$
$F \rightarrow ( E )$	$F.val = E.val$

# Inherited and Synthesized Attributes

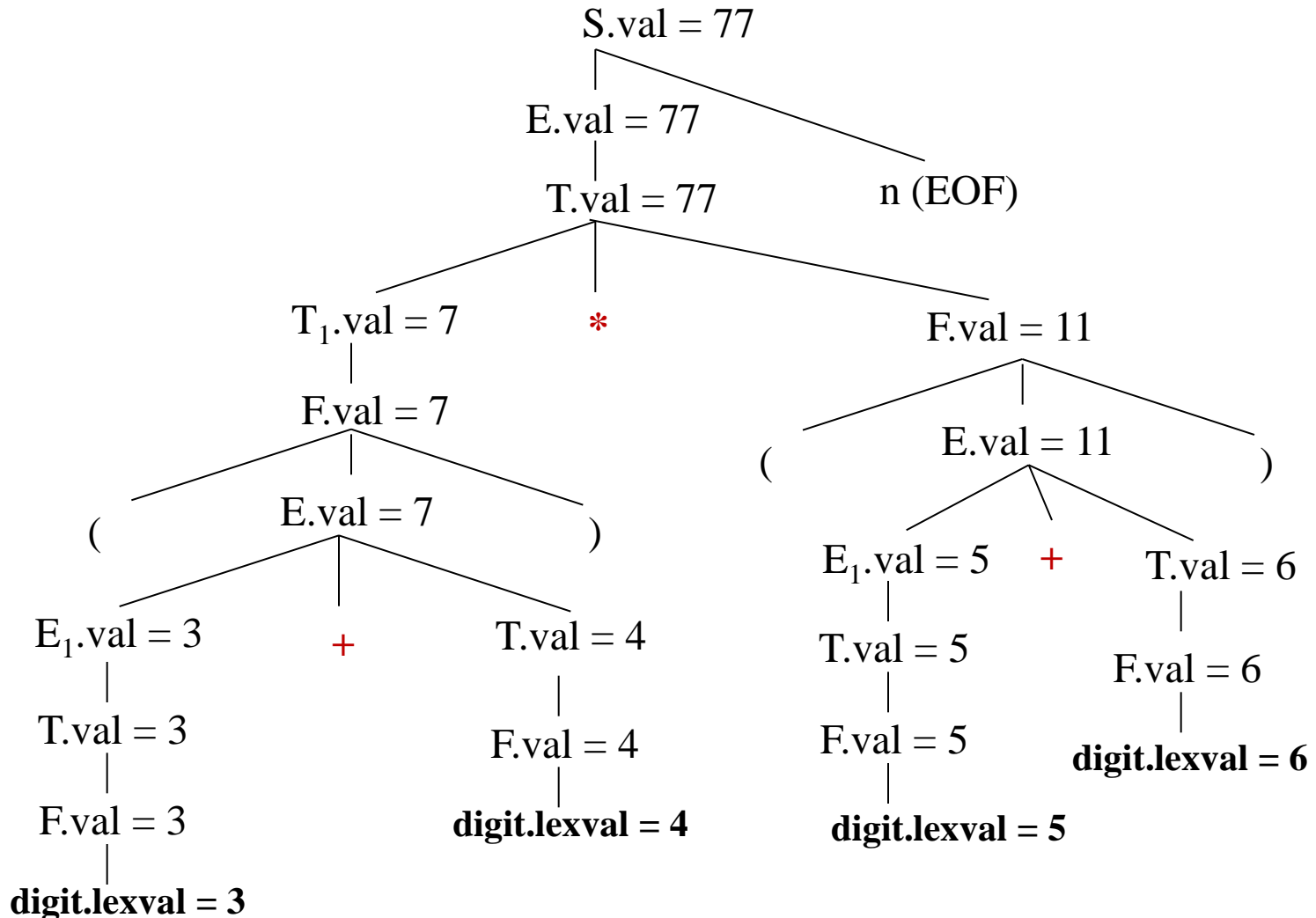
## Example: *Solution*

Now, the final SDD along with productions and semantic rules is shown below:

Productions	Semantic Rules
$S \rightarrow E_n$	$S.val = E.val$
$E \rightarrow E + T$	$E.val = E_1.val + T.val$
$E \rightarrow E - T$	$E.val = E_1.val - T.val$
$E \rightarrow T$	$E.val = T.val$
$T \rightarrow T * F$	$T.val = T_1.val * F.val$
$T \rightarrow T / F$	$T.val = T_1.val / F.val$
$T \rightarrow F$	$T.val = F.val$
$F \rightarrow ( E )$	$F.val = E.val$
$F \rightarrow \text{digit}$	$F.val = \text{digit.lexval}$

# Inherited and Synthesized Attributes

**Example:** The annotated parse tree for the expression  $(3+4)*(5+6)n$  consisting of attribute values for each non-terminal is shown below:



# Evaluating an SDD at the Nodes of a Parse Tree

We can easily obtain an **SDD** using the following steps:

**Step 1:** Construct the **parse tree**.

**Step 2:** Use the **rules** to **evaluate attributes** of all the **nodes** of the **parse tree**.

**Step 3:** Obtain the **attribute values** for each **non-terminal** and write the **semantic rules** for each **production**. When complete **annotated parse tree** is ready, we will have the **complete SDD**.

# Evaluating an SDD at the Nodes of a Parse Tree

*How do we construct an annotated parse tree?  
In what order do we evaluate attributes?*

- If we want to **evaluate** an **attribute** of a **node** of a **parse tree**, it is necessary to **evaluate** all the **attributes** upon which its **value depends**.
- If all **attributes** are **synthesized**, then we must **evaluate** the **attributes** of all of its **children** before we can evaluate **the attribute** of the **node** itself.
- With **synthesized** attributes, we can **evaluate** attributes in any **bottom up order**.
- Whether **synthesized** or **inherited** attributes there is **no single order** in which the **attributes** have to be **evaluated**. There can be **one** or **more orders** in which the **evaluation** can be done.

# Evaluating an SDD at the Nodes of a Parse Tree

## *Circular dependency*

- If the **attribute value** of a **parent node** depends on the **attribute value of child node** and **vice-versa**, then we say, there exists a **circular dependency** between the **child node** and **parent node**. In this situation, it is not possible to evaluate the attribute of either parent node or the child node since one value depends on another value.



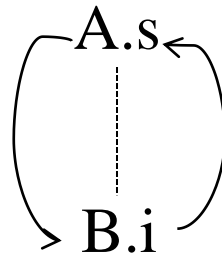
# Evaluating an SDD at the Nodes of a Parse Tree

## Circular dependency

- For example, consider the non-terminal **A** with synthesized attribute **A.s** and non-terminal **B** with inherited attribute **B.i** with following productions and semantic rules:

Productions	Semantic Rules
<b>A</b> → <b>B</b>	<b>A.s</b> = <b>B.i</b> <b>B.i</b> = <b>A.s</b> + 6

Partial annotated parse tree:



# Evaluating an SDD at the Nodes of a Parse Tree

## *Circular dependency*

Productions	Semantic Rules
$A \rightarrow B$	$A.s = B.i$ $B.i = A.s + 6$

- In the above semantic rule  $s$  is **synthesized attribute** and  $i$  is **inherited attribute**.
- The above two semantic rules are circular in nature.
- To compute  $A.s$  we require the values of  $B.i$  and to compute the value of  $B.i$ , we require the value of  $A.s$ . So, it is impossible to evaluate either the value of  $A.s$  or the value of  $B.i$  without evaluating other.

# Evaluating an SDD at the Nodes of a Parse Tree

## *Why evaluate inherited attributes*

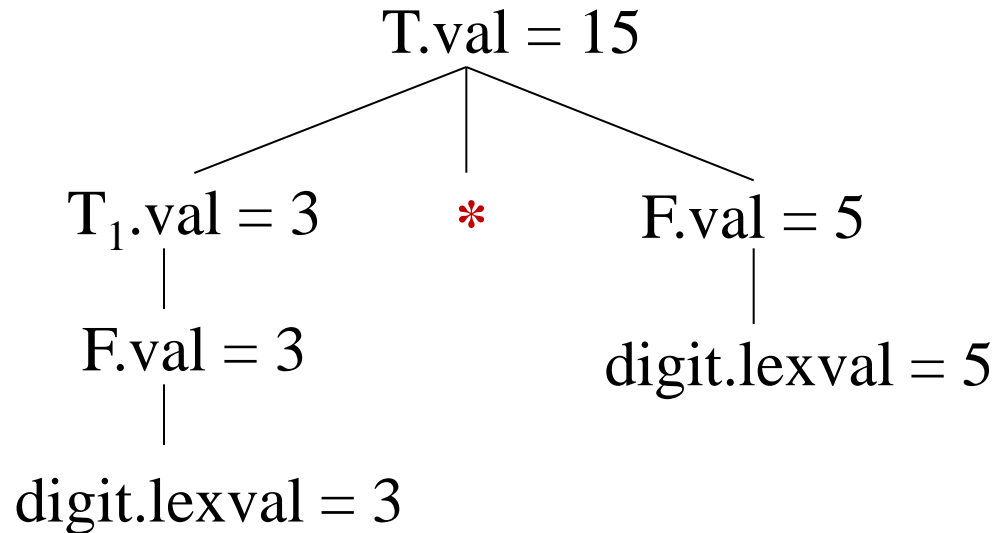
Consider the following grammar

$$T \rightarrow T * F \mid F$$
$$F \rightarrow \text{digit}$$

Using the above productions we can generate an **un-parenthesized expression** consisting of only **\*** operator such as: **3\*4** or **3\*4\*5** etc. The above grammar has **left-recursion** and it is suitable for **bottom up parser** such as **LR parser**. The **annotated parse tree** for evaluating the expression **3\*5** is shown below:

# Evaluating an SDD at the Nodes of a Parse Tree

## *Why evaluate inherited attributes*



It is very easy to see how the values **3** and **5** are moved from bottom to top till we reach the root node to the value **15** as shown in the above tree.

# Evaluating an SDD at the Nodes of a Parse Tree

## Why evaluate inherited attributes

Semantic Rules	Productions
$F.val = digit.lexval$	$F \rightarrow id$
$T.val = F.val$	$T \rightarrow F$
$T.val = T_1.val * F.val$	$T \rightarrow T * F$

Thus using **bottom-up manner**, the values **3** and **5** are moved upwards to get the result **15** using the **semantic rules** associated with each production.

# Evaluating an SDD at the Nodes of a Parse Tree

## Example:

Obtain **SDD** for the following grammar using top-down approach:

**S** → **En**

**E** → **E + T** | **T**

**T** → **T \* F** | **F**

**F** → **( E )** | **digit**

and obtain **annotated parse tree** for the expression **(3 + 4) \* (5 + 6)n**

# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

The given grammar has **left recursion** and hence it is not suitable for **top-down parser**. To make it suitable for **top-down parsing**, we have to **eliminate left recursion**. After **eliminating left recursion**, the following grammar is obtained:

**S** → **En**

**E** → **TE'**

**E'** → **+TE' | ε**

**T** → **FT'**

**T'** → **\*FT' | ε**

**F** → **( E ) | digit**

# Evaluating an SDD at the Nodes of a Parse Tree

**Example:** *Solution*

**Note:**

The variables **S**, **E**, **T** and **F** are present both in given grammar and grammar obtained after eliminating left recursion. So, only for the variables **S**, **E**, **T** and **F** we use the attribute name **v** (stands for *val*) and for all other variables we use **s** for *synthesized attribute* and **i** for *inherited attribute*.



# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

Consider the following productions:

**S** → **En**

**F** → ( **E** ) | **digit**

They do not have left recursion and they are retained in the grammar which is obtained after eliminating left recursion. So, we can compute the attribute value of **LHS** (**head**) from the attribute value of **RHS** (i.e., **children**) for the above productions and hence they have **synthesized attributes**.

# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

The productions, semantic rules and type of the attribute are shown below:

Production	Semantic Rule	Type
$S \rightarrow E n$	$S.v = E.v$	Synthesized
$F \rightarrow ( E )$	$F.v = E.v$	Synthesized
$F \rightarrow d$	$F.v = \text{digit.lexval}$	Synthesized

# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

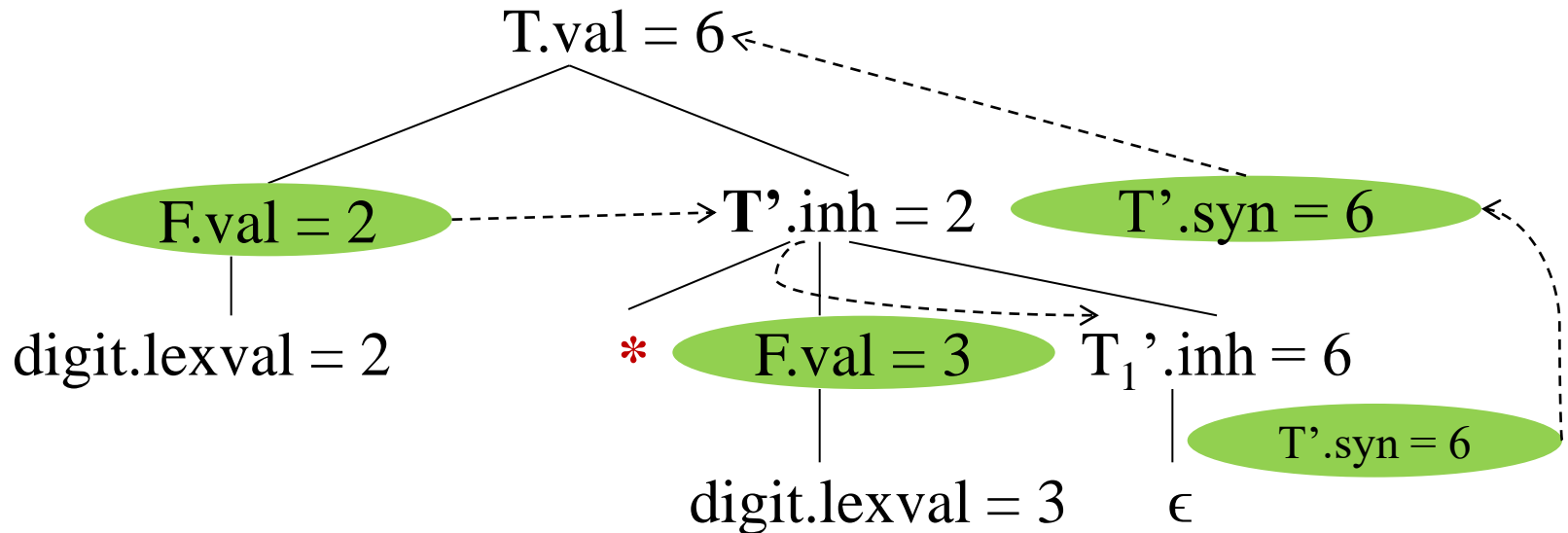
Consider the following productions and draw the **annotated parse tree** for the expression **2\*3** with flow of information as shown below:

Productions
$T \rightarrow F T'$
$T' \rightarrow * F T' \mid \epsilon$
$F \rightarrow \text{digit}$

# Evaluating an SDD at the Nodes of a Parse Tree

**Example:** *Solution*

Annotated parse tree for the expression **2\*3**:



# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

By following the **dotted arrow lines**, we can write the various **semantic rules** for the **corresponding productions** as shown below:

	Semantic Rule	Production
$F.val = 2$ is copied to $T'.inh$	$T'.inh = F.val$	$T \rightarrow F T'$
$T'.inh * F.val$ is copied to $T_1'.inh$	$T_1'.inh = T'.inh * F.val$	$T' \rightarrow * F T'$
$T_1'.inh$ is copied to $T'.syn$	$T'.syn = T_1'.inh$	$T' \rightarrow \epsilon$
$T'.syn$ is moved to its parent	$T'.syn = T_1'.syn$	$T' \rightarrow * F T'$
$T'.syn$ is moved to its parent $T$	$T.val = T'.syn$	$T \rightarrow F T'$

# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

The above productions and their respective rules along with the type of attribute are shown below:

Production	Semantic Rules
$T \rightarrow F T'$	$T'.inh = F.val$ $T.val = T'.syn$
$T' \rightarrow * F T'$	$T_1'.inh = T'.inh * F.val$ $T'.syn = T_1'.syn$
$T' \rightarrow \epsilon$	$T'.syn = T_1'.inh$

# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

Similar to the above, we can write the semantic rules for the other productions as shown below:

Production	Semantic Rules
$E \rightarrow T E'$	$E'.inh = T.val$ $E.val = E'.syn$
$E' \rightarrow + T E'$	$E_1'.inh = E'.inh + T.val$ $E'.syn = E_1'.syn$
$E' \rightarrow \epsilon$	$E'.syn = E_1'.inh$

# Evaluating an SDD at the Nodes of a Parse Tree

## Example: *Solution*

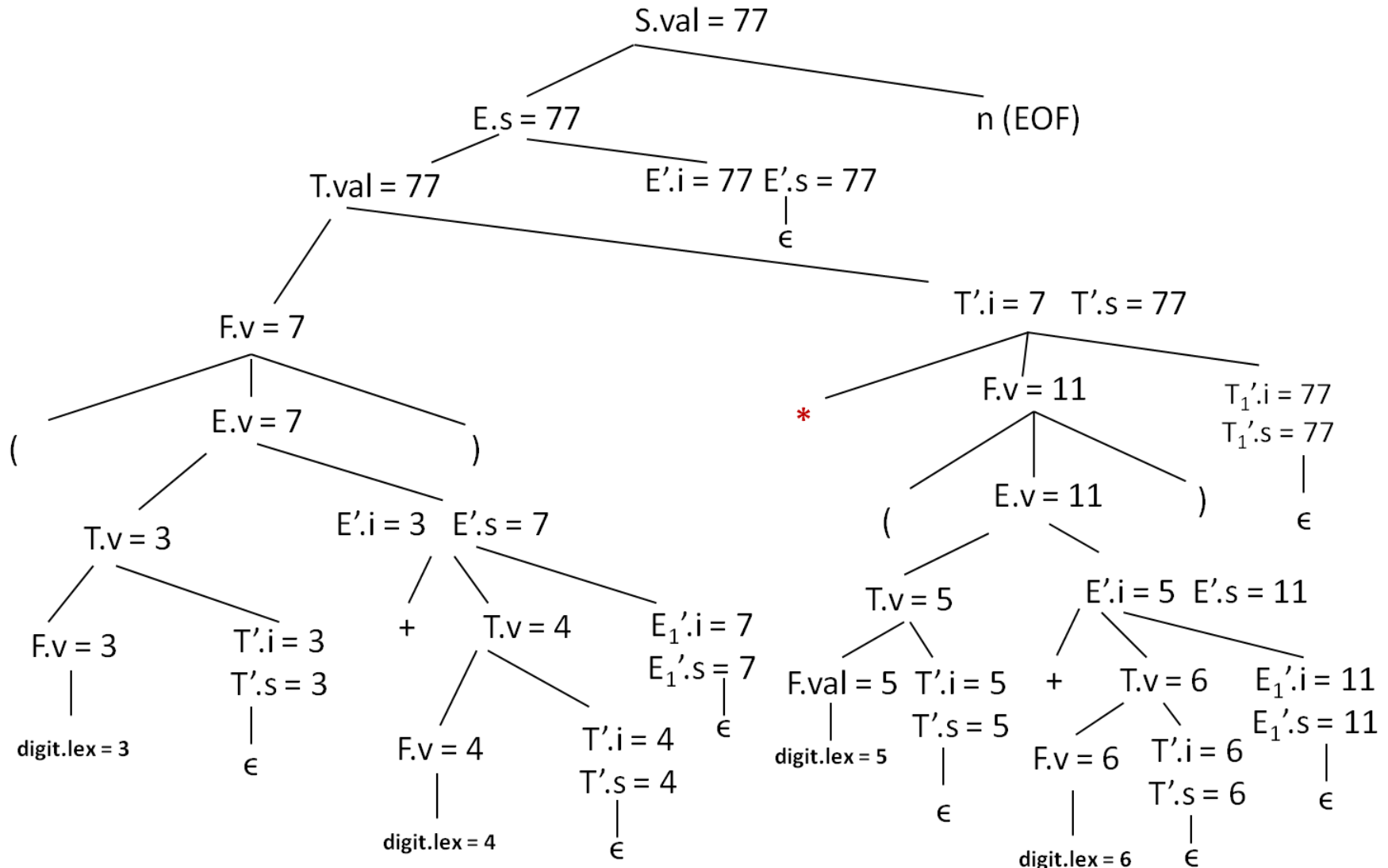
Combining all productions and semantic rules, we can write the final **SDD** as shown below:

Production	Semantic Rule	Type
$S \rightarrow E n$	$S.v = E.v$	Synthesized
$E \rightarrow T E'$	$E'.inh = T.val$	Inherited
	$E.val = E'.syn$	Synthesized
$E' \rightarrow + T E'$	$E_1'.inh = E'.inh + T.val$	Inherited
	$E'.syn = E_1'.syn$	Synthesized
$E' \rightarrow \epsilon$	$E'.syn = E_1'.inh$	Synthesized
$T \rightarrow F T'$	$T'.inh = F.val$	Inherited
	$T.val = T'.syn$	Synthesized
$T' \rightarrow * F T'$	$T_1'.inh = T'.inh * F.val$	Inherited
	$T'.syn = T_1'.syn$	Synthesized
$T' \rightarrow \epsilon$	$T'.syn = T_1'.inh$	Synthesized
$F \rightarrow ( E )$	$F.v = E.v$	Synthesized
$F \rightarrow d$	$F.v = digit.lexval$	Synthesized



# Evaluating an SDD at the Nodes of a Parse Tree

The **annotated parse tree** that shows the values of each attribute value while evaluating the expression  $(3+4) * (5+6)$  is shown below:



# Summary...

## Syntax-Directed Definitions (SDD)

- Inherited and Synthesized Attributes
- Evaluating an SDD at the Nodes of a Parse Tree

*Reading:* Aho2, Section 5.1.1 & 5.1.2

*Next Lecture:* Evaluation Orders for SDD's