THEORY OF COMPUTATION AND COMPILERS

Unit - II CONTEXT FREE GRAMMARS AND PARSING

- Introduction
- Context-Free Grammars Derivation, Parse trees, Ambiguity
- Types of Parsers
- LL(K) grammars and LL(1) parsing
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Unit-II: Syntax Analysis (or) Parser Using Ambiguous Grammars

Outline:

- Precedence and Associativity to Resolve Conflicts
- The "Dangling-Else" Ambiguity
- Error Recovery in LR parsing

Using Ambiguous Grammars

- Strictly speaking no LALR parser exists for ambiguous grammar.
- But, certain types of **ambiguous grammars** are quite useful in the specification and implementation of languages.
- For large constructs like expressions, an ambiguous grammar provides a shorter, more natural specification than any equivalent unambiguous grammar.

Using Ambiguous Grammars

- Even, for if-else construct, an ambiguous grammar provides more natural specification than its unambiguous grammar.
- Since, we are using ambiguous grammar to construct LR parsers, conflicts occur in the action part since there will be multiple entries in the parse table.

Using Ambiguous Grammars

The conflicts can be avoided as shown below:

- Using precedence and associativity to resolve the conflicts (In case of an expression)
- Avoiding dangling-else ambiguity

Example:

Obtain the LR parsing table for the following ambiguous grammar:

- $\mathbf{E'} \rightarrow \mathbf{E}$ where \$ indicates end of the input $\mathbf{1} \cdot \mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}$
- $2.E \rightarrow E \star E$
- $3.E \rightarrow (E)$
- $4.E \rightarrow id$

```
Example: Solution
```

The LR (0) items for the above augmented grammar can be computed as in SLR and are shown below:

```
I_0:
E' \rightarrow .E
E \rightarrow .E + E
E \rightarrow .E * E
E \rightarrow .(E)
E \rightarrow .id
```

```
Example: Solution
I_1: GOTO (I_0, E)
\mathbf{E'} \rightarrow \mathbf{E}.
\mathbf{E} \rightarrow \mathbf{E} \cdot \mathbf{+E}
\mathbf{E} \rightarrow \mathbf{E}. * \mathbf{E}
I_2: GOTO (I_0, ()
\mathbf{E} \rightarrow (\mathbf{E})
\mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}
\mathbf{E} \rightarrow \mathbf{E} \star \mathbf{E}
\mathbf{E} \rightarrow . (\mathbf{E})
\mathbf{E} \rightarrow .id
```

```
Example: Solution
I_3: GOTO (I_0, id)
\mathbf{E} \rightarrow \mathbf{id}.
I_4: GOTO (I_1, +)
\mathbf{E} \rightarrow \mathbf{E} + .\mathbf{E}
\mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}
\mathbf{E} \rightarrow \mathbf{E} \times \mathbf{E}
\mathbf{E} \rightarrow . (\mathbf{E})
\mathbf{E} \rightarrow .id
```

Example: Solution I_5 : GOTO (I_1 , *) $\mathbf{E} \rightarrow \mathbf{E} \star . \mathbf{E}$ $\mathbf{E} \rightarrow .\mathbf{E} + \mathbf{E}$ $\mathbf{E} \rightarrow \mathbf{E} \star \mathbf{E}$ $\mathbf{E} \rightarrow . (\mathbf{E})$ $\mathbf{E} \rightarrow .id$ I_6 : GOTO (I_2 , E) $\mathbf{E} \rightarrow (\mathbf{E}.)$ $\mathbf{E} \rightarrow \mathbf{E} \cdot \mathbf{+} \mathbf{E}$

 $\mathbf{E} \rightarrow \mathbf{E}$. * \mathbf{E}

```
Example: Solution
GOTO (I_2, () = I_2)
\mathbf{E} \rightarrow (\mathbf{E})
\mathbf{E} \rightarrow .\mathbf{E} + \mathbf{E}
\mathbf{E} \rightarrow \mathbf{E} \star \mathbf{E}
\mathbf{E} \rightarrow . (\mathbf{E})
\mathbf{E} \rightarrow .id
GOTO (I_2, id) = I_3
\mathbf{E} \rightarrow \mathbf{id}.
```

Example: Solution I_7 : GOTO (I_4 , E) $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}$. $\mathbf{E} \rightarrow \mathbf{E} \cdot \mathbf{+E}$ $\mathbf{E} \rightarrow \mathbf{E} \cdot \mathbf{\times} \mathbf{E}$ GOTO $(I_4, () = I_2)$ $\mathbf{E} \rightarrow (\mathbf{E})$ $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}$ $\mathbf{E} \rightarrow \mathbf{E} \times \mathbf{E}$ $\mathbf{E} \rightarrow . (\mathbf{E})$ $\mathbf{E} \rightarrow .id$

```
Example: Solution
GOTO (I_4, id) = I_3
\mathbf{E} \rightarrow \mathbf{id}.
I_8:GOTO (I_5, E)
\mathbf{E} \rightarrow \mathbf{E} \star \mathbf{E}.
\mathbf{E} \rightarrow \mathbf{E} \cdot \mathbf{+} \mathbf{E}
\mathbf{E} \rightarrow \mathbf{E} \cdot \mathbf{\times} \mathbf{E}
GOTO (I_5, () = I_2)
GOTO (I_5, id) = I_3
I_9: GOTO (I_6, ))
\mathbf{E} \rightarrow (\mathbf{E}).
```

Example: Solution

```
GOTO (I_6, +) = I_4

GOTO (I_6, *) = I_5

GOTO (I_7, +) = I_4

GOTO (I_7, *) = I_5

GOTO (I_8, +) = I_4

GOTO (I_8, *) = I_5
```

Example: Solution

The **FIRST** and **FOLLOW** sets for the given grammar can be obtained as shown below:

	E			
FIRST	(, id			
FOLLOW	+,*,),\$			

Example: Solution

Construction of SLR Parsing Table:

The parsing action function **ACTION** and **GOTO** can be obtained as shown below:

Example: Solution

The **ACTION** entries for terminals can be obtained as shown below: **Algorithm Rule 2.a**

Transition GOTO $(I_i, a) = I_j$	ACTION [i, a] = shift j
$I_0, (= I_2)$	$[0, (] = s_2$
I_0 , id = I_3	$[0, id] = s_3$
$I_1, + = I_4$	$[1, +] = s_4$
$I_1, * = I_5$	$[1, *] = s_5$
$I_2, (= I_2)$	[2, (] = s2

Example: Solution

Construction of SLR Parsing Table:

Transition GOTO $(I_i, a) = I_j$	ACTION [i, a] = shift j
I_2 , id = I_3	$[2, id] = s_3$
$I_4, (= I_2$	$[4, (] = s_2$
I_4 , id = I_3	$[4, id] = s_3$
I_5 , (= I_2	[5, (] = s2
I_5 , id = I_3	$[5, id] = s_3$

Example: Solution

Construction of SLR Parsing Table:

Transition GOTO $(I_i, a) = I_j$	ACTION [i, a] = shift j
$I_6, + = I_4$	$[6, +] = s_4$
I_6 , $\star = I_5$	$[6, *] = s_5$
$I_6,) = I_9$	$[6,)] = s_9$
$I_7, + = I_4$	$[7, +] = s_4$
I_7 , $\star = I_5$	$[7, *] = s_5$
I_8 , $+ = I_4$	$[8, +] = s_4$
I_8 , $\star = I_5$	$[8, *] = s_5$

Example: Solution

The **ACTION** entries for the items ending with dot (.) are shown below: **Algorithm Rule 2.b**

[7 ~ 1cT	a = FOLLOW (A) then
$[A \rightarrow \alpha.] \in I_{i}$	ACTION [i, a] = \mathbf{r} A \rightarrow α
[E → id.]∈I ₃	$[3, \{*, +,), \$\}] = r E \rightarrow id$
	$(i.e., r_4)$
	$FOLLOW (E) = \{*, +,), \$\}$
$[E \rightarrow E + E.] \in I_7$	$[7, \{*, +,), \$\}] = r_1$

Example: Solution

```
\begin{bmatrix} \mathbf{A} \rightarrow \alpha . \ ] \in \mathbf{I_i} \\ \mathbf{ACTION} \ [\mathbf{i}, \ \mathbf{a}] = \mathbf{r} \ \mathbf{A} \rightarrow \alpha \\ \begin{bmatrix} \mathbf{E} \rightarrow \mathbf{E} & \mathbf{E} . \ ] \in \mathbf{I_8} \\ \mathbf{E} \rightarrow \mathbf{E} & \mathbf{E} . \end{bmatrix} \in \mathbf{I_8} \begin{bmatrix} \mathbf{8}, \ \{*, +, ), \ \$\} \end{bmatrix} = \mathbf{r_2} \\ \begin{bmatrix} \mathbf{E} \rightarrow \mathbf{C} & \mathbf{E} \\ \mathbf{E} \rightarrow \mathbf{E} & \mathbf{E} \end{bmatrix} \in \mathbf{I_9} \begin{bmatrix} \mathbf{9}, \ \{*, +, ), \ \$\} \end{bmatrix} = \mathbf{r_3} \end{bmatrix}
```

```
Example: Solution [S' \rightarrow S.] \in I_i then ACTION [i, \$] = accept: Algorithm Rule 2.c
```

Example: Solution

The **GOTO** states can be computed using <u>rule-3</u> are shown below: **Algorithm Rule 3**

Transition	Table		
$ GOTO (I_i, A) = I_j$	GOTO $[i, A] = j$		
I_0 , $E = I_1$	[0, E] = 1		
I_2 , $E = I_6$	[2, E] = 6		
I_4 , $E = I_7$	[4, E] = 7		
I_5 , $E = I_8$	[5, E] = 8		

Example: The final SLR parsing table:

	ACTION						GOTO
	id	+	*	()	\$	E
0	S ₃			S ₂			1
1		S ₄	S ₅			acc	
2	S ₃			S ₂			6
3		r ₄	r ₄		r ₄	r ₄	
4	S ₃			S ₂			7
5	S ₃			S ₂			8
6		S ₄	S ₅		S ₉		
7		S ₄ , r ₁	S ₅ , r ₁	r_1		r ₁	
8		S ₄ , r ₂	S ₅ , r ₂	r ₂		r ₂	
9		r ₃	r ₃		r ₃	r ₃	
10							
11							

Example: Solution

Since the grammar is ambiguous, it results in parsingaction conflicts when we produce the parsing table as shown above.

The sates corresponding to I7 and I8 generates these conflicts on input symbols + and *.

How to avoid shift-reduce conflicts in a grammar that has arithmetic operators?

- These conflicts can be resolved using precedence and associativity of operators as shown below:
- 1. If input operator and prefix on top of the stack to be reduced have same precedence and if the operator is <u>left associative</u>, then preference is given for <u>reduction</u> action.

How to avoid shift-reduce conflicts in a grammar that has arithmetic operators?

2. If input operator and prefix on top of the stack to be reduced have same precedence and if the operator is right associative, then preference is given for shift action.

How to avoid shift-reduce conflicts in a grammar that has arithmetic operators?

- 3. If input operator has less precedence than the operator present in the prefix that has to be reduced, then preference is given for reduce action.
- 4. If input operator has higher precedence than the operator present in the prefix that has to be reduced, then preference is given for shift action.

In our example

• Consider the entry: action $(7, +) = s_4 \mid r_1$. The conflict is whether to shift 4 or to reduce using $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}$ (since \mathbf{r}_1 stands for reducer 1^{st} production). When the input symbol is + and stack contains **E** + **E** and since operator + is leftassociative, preference is given for reduction. So, retain \mathbf{r}_1 and eliminate \mathbf{s}_4 .

In our example

• Consider the entry: action $(7, *) = s_5 \mid r_1$. The conflict is whether to shift 5 or to reduce using $\mathbf{E} \rightarrow \mathbf{E} + \mathbf{E}$ (since \mathbf{r}_1 stands for reducer 1^{st} production). When the input symbol is * and stack contains **E** + **E** and since operator * has higher precedence than +, preference is given for shifting and not for reduction. So, retain s_5 and eliminate r_1 .

In our example

• Consider the entry: action $(8, +) = s_4 \mid r_2$. The conflict is whether to shift 4 or to reduce using $\mathbf{E} \rightarrow \mathbf{E} \star \mathbf{E}$ (since \mathbf{r}_2 stands for reducer 2^{nd} production). When the input symbol is + and stack contains **E** * **E** and since operator * higher precedence than +, preference is given for reduction and not for shifting. So, retain \mathbf{r}_2 and eliminate \mathbf{s}_4 .

In our example

• Consider the entry: action (8, *) = $s_5 \mid r_2$. The conflict is whether to shift 5 or to reduce using $\mathbf{E} \rightarrow \mathbf{E} \star \mathbf{E}$ (since \mathbf{r}_2 stands for reducer 2^{nd} production). When the input symbol is * and stack contains **E** * **E** and since operator * and stack contains **E** * **E** and since operator * is **left**associative, preference is given for reduction. So, retain \mathbf{r}_2 and eliminate \mathbf{s}_5 .

So, the final parsing table can be shown below:

	ACTION						GOTO
	id	+	*	()	\$	E
0	S ₃			S ₂			1
1		S ₄	S ₅			acc	
2	S_3			S ₂			6
3		r ₄	r ₄		r ₄	r ₄	
4	S ₃			S ₂			7
5	S ₃			S ₂			8
6		S ₄	S ₅		S ₉		
7		r ₁	S ₅	r ₁		r ₁	
8		r ₂	r ₂	r ₂		r ₂	
9		r ₃	r ₃		r ₃	r ₃	
10							
11							

Avoiding dangling-else ambiguity

Example:

Obtain the LR parsing table for the following ambiguous grammar:

- S' → S\$ where \$ indicates end of the input
- 1.S → iSeS
- $2.S \rightarrow iS$
- $3.S \rightarrow a$

Avoiding dangling-else ambiguity

Example: Solution

The LR (0) items for the above augmented grammar can be computed as in SLR and are shown below:

```
I_0:
S' \rightarrow .S
S \rightarrow .iSeS
S \rightarrow .iS
S \rightarrow .a
```

Avoiding dangling-else ambiguity

```
Example: Solution LR(0) items
I_1: GOTO (I_0, S)
S' \rightarrow S.
I_2: GOTO (I_0, i)
S → i.SeS
S \rightarrow i.S
S → .iSeS
S \rightarrow .iS
S \rightarrow .a
```

```
Example: Solution LR(0) items I_3: GOTO (I_0, a) S \rightarrow a. I_4: GOTO (I_2, S) S \rightarrow iS.eS S \rightarrow iS.
```

```
Example: Solution LR(0) items
GOTO (I_2, i) = I_2
S → i.SeS
S \rightarrow i.S
S → .iSeS
S \rightarrow .iS
S \rightarrow .a
GOTO (I_2, a) = I_3
S \rightarrow a.
```

```
Example: Solution LR(0) items
GOTO (I_2, a) = I_3
S \rightarrow a.
I_5:GOTO (I_4, e)
S → iSe.S
S → .iSeS
S \rightarrow .iS
S \rightarrow .a
```

```
Example: Solution LR(0) items I_6:GOTO (I_5, S) S \rightarrow iSeS.

GOTO (I_5, i) = I_2
GOTO (I_5, a) = I_3
```

Example: Solution FIRST and FOLLOW

The **FIRST** and **FOLLOW** sets for the given grammar can be obtained as shown below:

	S		
FIRST	i, a		
FOLLOW	e, \$		

Example: Solution SLR Parsing table construction

		GOTO			
	i	е	a	\$	S
0	S ₂		S ₃		1
1				acc	
2	S ₂		S ₃		4
3		r ₃		r ₃	
4		s _{5.} r ₂		r ₂	
5	S ₂	,	S ₃		6
6		r_1	r_1		

Example: Solution

Observe that there are <u>multiple entries</u> in the above **LR** parsing table, since the given grammar is ambiguous. In the entry at action $(4, e) = s_5 \mid r_2$ i.e., there is a conflict whether to shift 5 on to the stack or reduce using 2nd production i.e., $S \rightarrow iS$. If S is present on top of the stack instead of reducing, it is better to shift 5 which corresponds to else. This is because, the else is always associated with closest **if** and so instead of reducing, give preference for shifting. So, retain s_5 and eliminate r_2 .

Example: Solution Final SLR Parsing table is shown below:

	ACTION				GOTO
	i	е	a	\$	S
0	S ₂		S ₃		1
1				acc	
2	S ₂		S ₃		4
3		r ₃		r ₃	
4		S ₅		r ₂	
5	S ₂		S ₃		6
6		r ₁	r ₁		

- An LR parser will detect an error when it consults the parsing action table and finds an error entry.
- Errors are never detected by consulting the goto table.
- An LR parser will announce an error as soon as there is no valid continuation for the portion of the input thus far scanned.
- A canonical LR parser will not make even a single reduction before announcing an error.

- SLR and LALR parsers may make several reductions before announcing an error, but they will never shift an erroneous input symbol onto the stack.
- In LR parsing, we can implement panic-mode error recovery as follows.
- 1. We scan down the stack until a state s with a goto on a particular nonterminal A is found. Zero or more input symbols are then discarded until a symbol a is found that can follow A.

Panic-mode error recovery:

2. The parser then stacks the state GOTO (s, A) and resumes normal parsing. There might be more than one choice for the nonterminal A. Normally these would be nonterminals representing major program pieces, such as an expression, statement, or block. For example, if A is the nonterminal stmt, a might be **semicolon** or }, which marks the end of a statement sequence.

Panic-mode error recovery:

- 3. This method of recovery attempts to eliminate the phrase containing the syntactic error. The parser determines that a string derivable from A contains an error. Part of that string has already been processed, and the result of this processing is a sequence of states on top of the stack.
- 4. The remainder of the string is still in the input, and the parser attempts to skip over the remainder of this string by looking for a symbol on the input that can follow A.

Panic-mode error recovery:

5. By removing states from the stack, skipping over the input, and pushing GOTO (s, A) on the stack, the parser pretends that it has found an instance of A and resumes normal parsing.

Phrase-level recovery:

- 1. Phrase-level recovery is implemented by examining each error entry in the LR parsing table and deciding on the basis of language usage the most likely programmer error that would give rise to that error.
- 2. An appropriate recovery procedure can then be constructed; evidently the top of the stack and/or first input symbols would be modified in a way deemed appropriate for each error entry.

- In designing specific error-handling routines for an LR parser, we can fill in each blank entry in the action field with a pointer to an error routine that will take the appropriate action selected by the compiler designer.
- The actions may include insertion or deletion of symbols from the stack or the input or both, or alteration and transposition of input symbols.

- We must make our choices so that the LR parser will not get into an infinite loop.
- A safe strategy will assure that at least one input symbol will be removed or shifted eventually, or that the stack will eventually shrink if the end of the input has been reached.
- Popping a stack state that covers a nonterminal should be avoided, because this modification eliminates from the stack a construct that has already been successfully parsed.

Example:

Consider again the expression grammar:

- $1. E \rightarrow E + E$
- $2.E \rightarrow E \star E$
- $3.E \rightarrow (E) \mid id$

Example:

LR Parsing table for grammar is shown below:

	ACTION						GOTO
	id	+	*	()	\$	E
0	S ₃			S ₂			1
1		S ₄	S ₅			acc	
2	S ₃			S ₂			6
3		r ₄	r ₄		r ₄	r ₄	
4	S ₃			S ₂			7
5	S ₃			S ₂			8
6		S ₄	S ₅		S ₉		
7		r ₁	S ₅		r_1	r ₁	
8		r ₂	r ₂		r ₂	r ₂	
9		r ₃	r ₃		r ₃	r ₃	

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Example:

The LR parsing table modified for error detection and recovery.

	ACTION					GOTO	
	id	+	*	()	\$	E
0	S ₃	e_1	e_1	S ₂	e ₂	e_1	1
1	e ₃	S ₄	S ₅	e ₃	e ₂	acc	
2	S ₃	e_1	e_1	S ₂	e ₂	$\mathbf{e_1}$	6
3	r ₄						
4	S_3	$\mathbf{e_1}$	e_1	S ₂	e ₂	$e_{\scriptscriptstyle 1}$	7
5	S_3	$\mathbf{e_1}$	e_1	S ₂	e ₂	$e_{\scriptscriptstyle 1}$	8
6	e ₃	S_4	S ₅	e ₃	S ₉	$\mathbf{e_4}$	
7	r ₁	r_1	S ₅	r_1	r ₁	r_1	
8	r ₂						
9	r ₃						

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Example: Error descriptions

e1: This routine is called from states 0, 2, 4 and 5, all of which expect the beginning of an operand, either an id or a left parenthesis. Instead, +, *, or the end of the input was found.

push state 3 (the goto of states 0, 2, 4 and 5 on id); issue diagnostic "missing operand."

Example: Error descriptions

e2: Called from states 0, 1, 2, 4 and 5 on finding a right parenthesis.

remove the right parenthesis from the input; issue diagnostic "unbalanced right parenthesis."

Example: Error descriptions

e3: Called from states 1 or 6 when expecting an operator, and an id or right parenthesis is found.

push state 4 (corresponding to symbol +) onto the stack;
issue diagnostic "missing operator."

Example: Error descriptions

e4: Called from state 6 when the end of the input is found.

push state 9 (for a right parenthesis) onto the stack; issue diagnostic "missing right parenthesis."

Summary...

Bottom-Up Parsing: Using Ambiguous Grammars

- Precedence and Associativity to Resolve Conflicts
- The "Dangling-Else" Ambiguity
- Error Recovery in LR parsing

Reading: Aho2, Section 4.8 (4.8.1, 4.8.2 & 4.8.3) & 4.6.5

Next Lecture: Parser Generators