


THEORY OF COMPUTATION AND COMPILERS

Unit - II

CONTEXT FREE GRAMMARS AND PARSING

- Introduction
- Context-Free Grammars - Derivation, Parse trees, Ambiguity
- **Types of Parsers** 
- LL(K) grammars and LL(1) parsing
- Bottom-up Parsing - handle pruning
- LR Grammar Parsing
- LALR parsing
- Parsing ambiguous grammars
- Error Recovery in Parsing
- YACC programming specification

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Unit-II: Syntax Analysis (or) Parser

Top-Down Parsing

Outline:

- Top-Down Parsing-Introduction
- Recursive-Descent Parsing
- Recursive-descent parser with backtracking
- Difficulties in Top-Down Parser

Top-Down Parsing

Definition:

Construction of the **parse tree** starts at the **root** (from the **start symbol**) and proceeds towards **leaves** (**tokens** or **terminals**). i.e., construction of the **parse tree** is done from **top** to **bottom** of the tree.

(or)

Construction of the **parse tree** from the **root** (**starting non-terminal**) to the **leaves** in **pre-order** in **depth-first search** manner for the given input string.

Top-Down Parsing

- Thus, **top-down parsing** can be viewed as an attempt to find a **leftmost derivation** for an input string and constructing the **parse tree** for that derivation. The **parser** that uses this approach is called **top-down parsing**.

Top-Down Parsing

Example-1:

Show the **top-down parsing** process for the string **id+id*id** for the grammar given below:

E → **E + E**

E → **E * E**

E → **(E)**

E → **id**

Top-Down Parsing

Example: Solution

Leftmost Derivation (LMD):

$$E \Rightarrow_{lm} E + E$$

$$E \Rightarrow_{lm} id + E [E \rightarrow id]$$

$$E \Rightarrow_{lm} id + E * E [E \rightarrow E * E]$$

$$E \Rightarrow_{lm} id + id * E [E \rightarrow id]$$

$$E \Rightarrow_{lm} id + id * id [E \rightarrow id]$$

Productions
$E \rightarrow E + E \mid E * E \mid (E) \mid id$

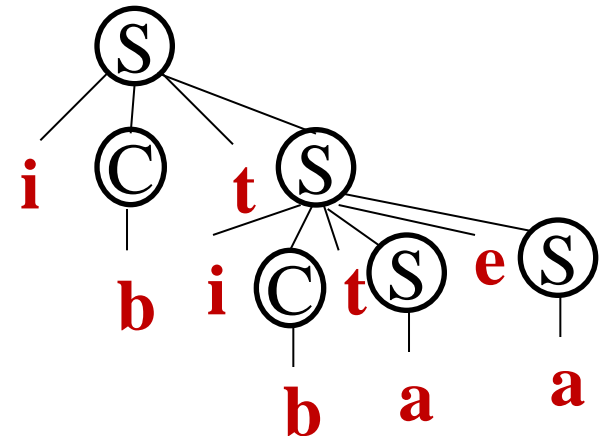
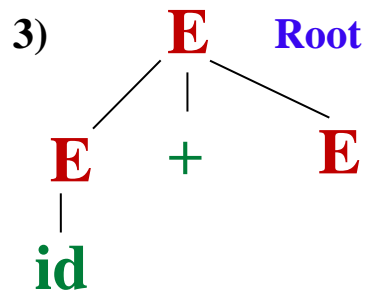
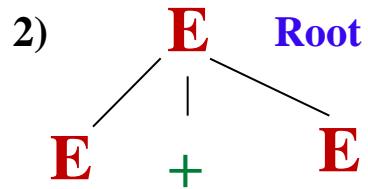


Fig: Parse tree for the LMD1 of string **ibtibtaea**

Top-Down Parsing

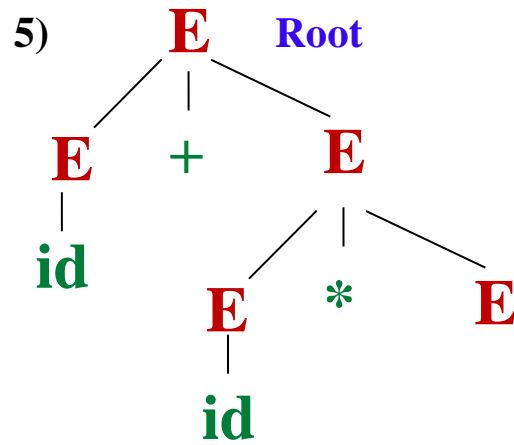
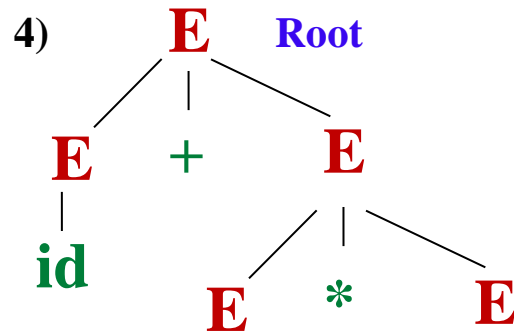
Example: Solution

1) **E** Root



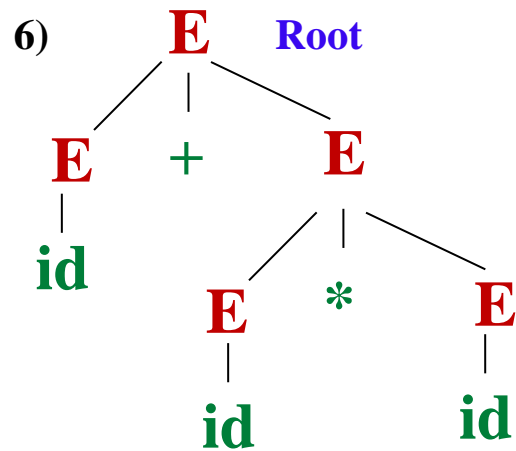
Top-Down Parsing

Example: Solution



Top-Down Parsing

Example: Solution



Top-Down Parsing

Practice Problem:

Show the **top-down parsing** process for the string **id+id*id** for the grammar given below:

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \epsilon$$

$$F \rightarrow (E) \mid id$$

Recursive-Descent Parsing

- A **recursive-descent parser** is a **top-down parser** in which **parse tree** is constructed from the top starting from **root node** and selecting the productions from the **left to right** (If two or more alternative productions exists).
- For every **non-terminal** there exist a **recursive procedure** and the right hand side of the production of that **non-terminal** is implemented as the **body of the procedure**.

Recursive-Descent Parsing

- The sequence of **terminals** and **non-terminals** on the **right hand side** of the production correspond to matching with **input** symbols and calls to **other procedures** while selecting the **alternate production** is implemented using **switch** or **if**-statements.
- For example, the procedure for the production $A \rightarrow \alpha$ can be written as shown below:

```
Procedure A() //Function header
{
... } //body of the function
...
}
```

Recursive-Descent Parsing

General procedure for a recursive-descent parsing:

A typical procedure for a nonterminal in a top-down parser for the production $\mathbf{A} \rightarrow \mathbf{X}_1\mathbf{X}_2\mathbf{X}_3 \dots \mathbf{X}_k$ can be written as shown below

(backtracking is not supported):

Procedure $\mathbf{A}()$ {

 Choose an \mathbf{A} -production, $\mathbf{A} \rightarrow \mathbf{X}_1\mathbf{X}_2\mathbf{X}_3 \dots \mathbf{X}_k$

 for ($\mathbf{i} = 1$ to \mathbf{k}) {

 if (\mathbf{X}_i is a nonterminal)

 call procedure $\mathbf{X}_i()$;

 else if (\mathbf{X}_i equals the current input symbol \mathbf{a})

 advance the input to the next symbol;

 else /* an error has occurred */;

 }

}

Recursive-Descent Parsing

Example:

Write the recursive-descent parser procedure for the following grammar:

$$E \rightarrow T$$
$$T \rightarrow F$$
$$F \rightarrow (E) \mid id$$

Recursive-Descent Parsing

Example: *Solution*

// Procedure corresponding to the production $E \rightarrow T$

Procedure $E()$

{

$T()$;

}

Recursive-Descent Parsing

Example: *Solution*

// Procedure corresponding to the production $\mathbf{T} \rightarrow \mathbf{F}$

Procedure $\mathbf{T}()$

{

$\mathbf{F}()$;

}

Recursive-Descent Parsing

Example: *Solution*

/ Procedure corresponding to the production $F \rightarrow (E) \mid id$ */*

```
Procedure F() {  
    if (input_symbol == '(')  
        advance input_pointer;  
    E();  
    if (input_symbol == ')')  
        advance input_pointer;  
    else  
        error();  
    end if  
    else if (input_symbol == 'id')  
        advance input_pointer;  
    else  
        error();  
    end if  
}
```

Recursive-Descent Parsing

Types of recursive-descent parsers:

1. A **recursive-descent parser** with **backtracking**
2. A **recursive-descent parser** without **backtracking (Predictive Parser)**

Recursive-Descent Parsing

Recursive-descent parser with backtracking:

The **backtracking** is necessary for the following reasons:

1. During **parsing**, the productions are applied one by one. But if two or more alternative productions are there, they are applied in order from left to right one at a time.

Recursive-Descent Parsing

Recursive-descent parser with backtracking:

2. When a particular production applied fails to expand the nonterminal properly, we have to apply the alternative production, it is necessary *undo* the activities done using the current production. This is possible only using **backtracking**.
3. But the **recursive-descent parser** with backtracking are not frequently used.

Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example:

Show the steps involved in recursive-descent parser with backtracking for the input string **cad** for the following grammar:

S → **cAd**

A → **ab** | **a**

Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example: *Solution*

Given grammar:

S → **cAd**

A → **ab** | **a**

String to be parsed:

cad

Parse tree:

S (**root**)

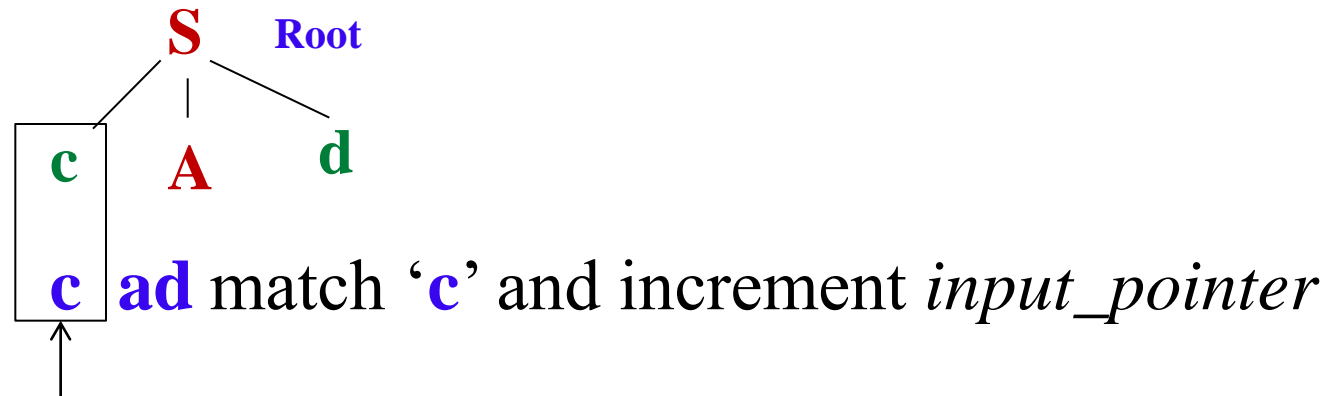
↑ *input pointer*

Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example: *Solution*

Step-1:

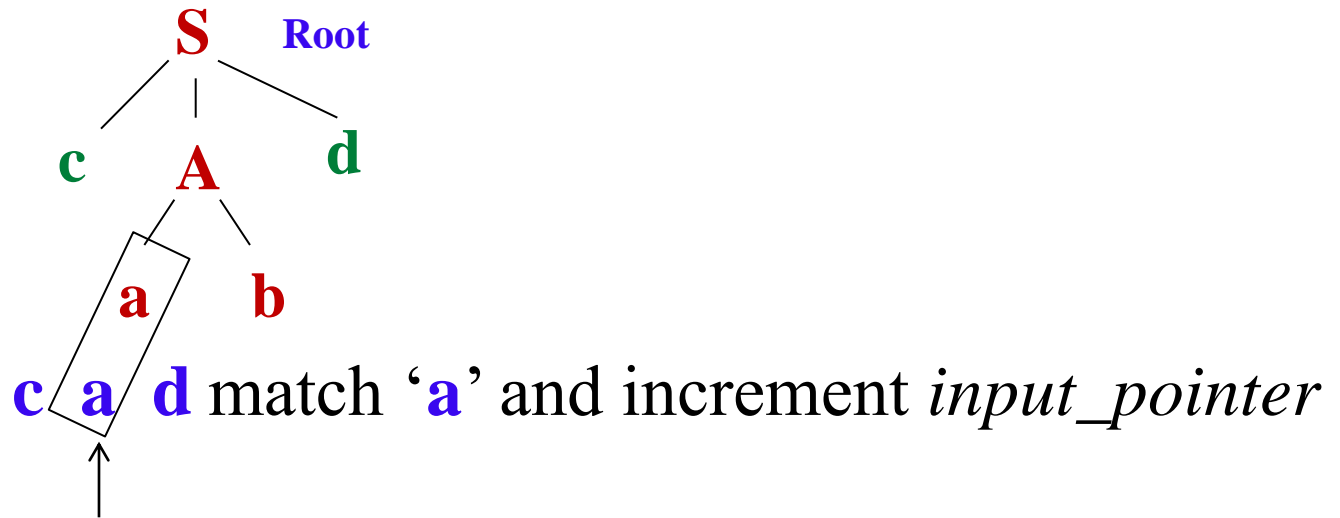


Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example: *Solution*

Step-2:

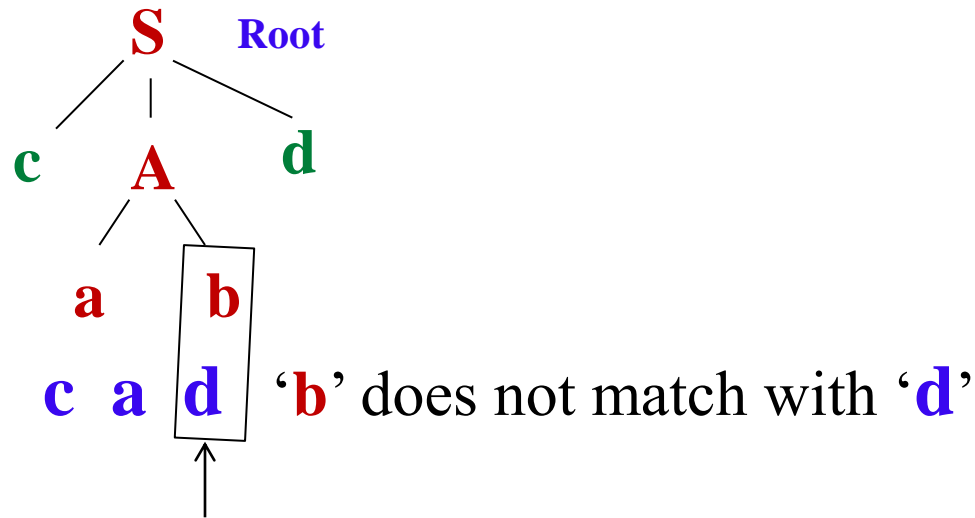


Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example: *Solution*

Step-3:



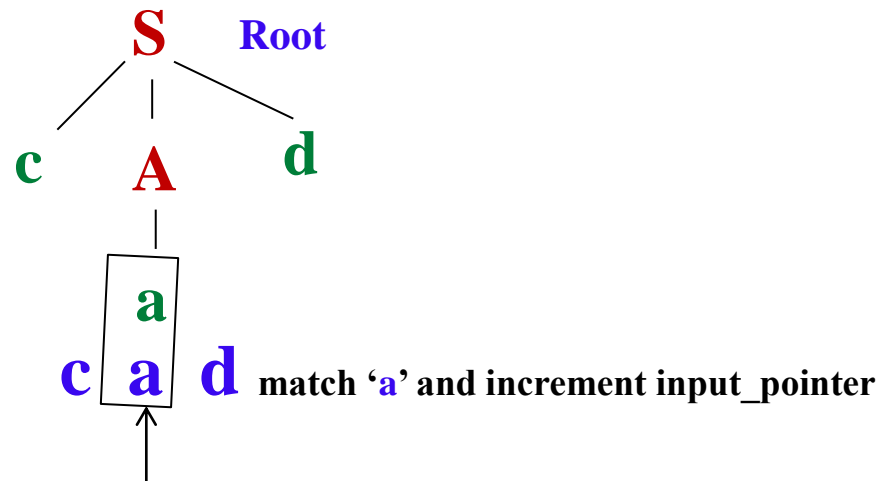
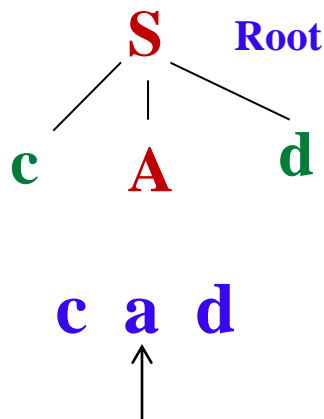
Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example: Solution

Step-4 :

By selecting $A \rightarrow ab$ the input string is not matched. So we have to reset the pointer to input symbol 'a'. This is done using **backtracking** is shown below:



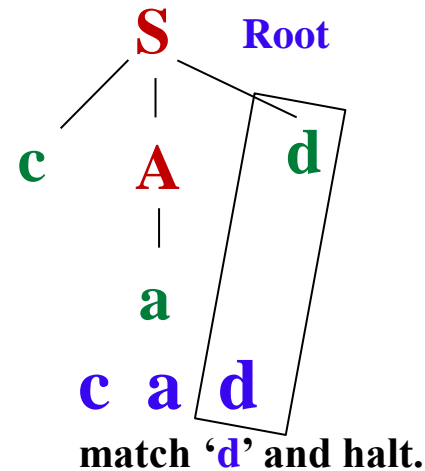
Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Example: *Solution*

Step-5:

Now the next symbol '**d**' in grammar is compared with '**d**' in the input and they *match*. Finally, we halt and announce **successful completion of parsing**.



Recursive-Descent Parsing

Recursive-descent parser with backtracking:

Recursive descent-parser cannot be constructed for a grammar having:

- 1. Ambiguity:** The solution is to eliminate ambiguity from the grammar.
- 2. Left recursion:** The solution is to eliminate left recursion from the grammar.
- 3. Left factoring:** Two or more alternatives having a common prefix. The solution is to left factor the grammar.

Recursive-Descent Parsing

Difficulties in Top-Down Parser:

1. **Ambiguity:** Not suitable for top-down parser.
2. **Left recursion:** Not suitable for top-down parser.
3. **Non-left factored grammar:** Left factoring is must for top-down parser.
4. **Backtracking:** The backtracking is necessary for top-down parser.

Backtracking parsers are more powerful than **predictive parsers**, they are also much slower, requiring exponential time in general and therefore, **backtracking parsers** are not suitable for **practical compilers**.

Summary...

Top-Down Parsing : Recursive-Descent Parser

- Top-Down Parsing-Introduction
- Recursive-Descent Parsing
- Recursive-descent parser with backtracking
- Difficulties in Top-Down Parser

Reading: Aho2, Section 4.3

Next Lecture: Predictive parser (or) Non-Recursive-Descent Parser